



# Cryptography

## Lecture 1

*Dr. Panagiotis Rizomiliotis*

# Agenda

- Introduction
- History of cryptography
- Crypto agenda

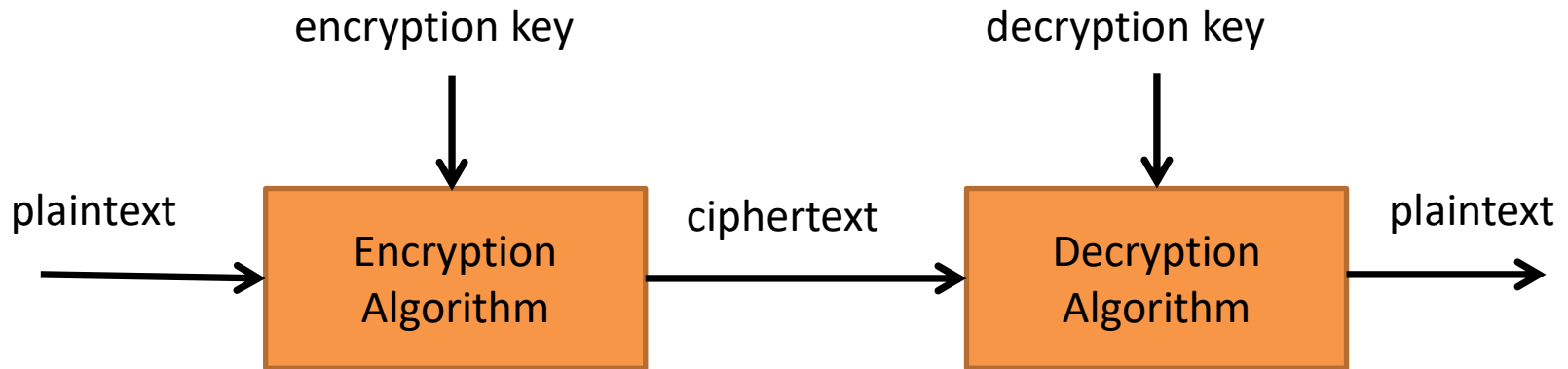
# definitions

- Cryptography
- Cryptanalysis
- Cryptology
- Cryptosystem

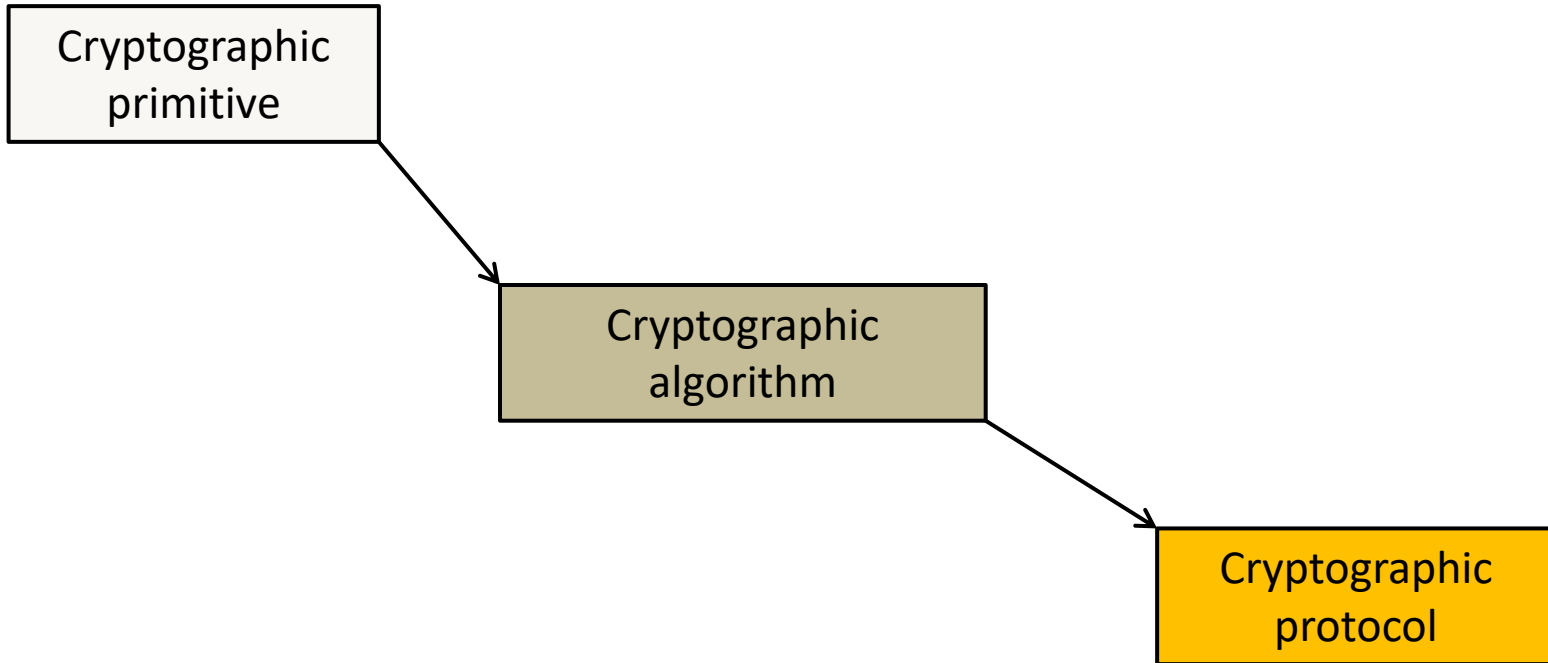


ΚΡΥΠΤΟΓΡΑΦΙΑ

# Basic model of a cryptosystem

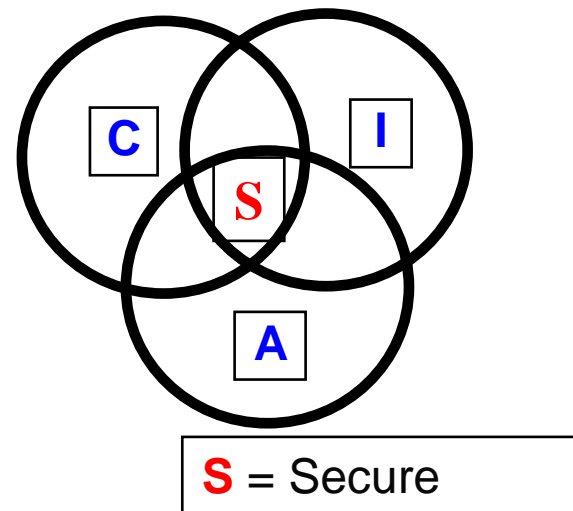


# (more) definitions



# Traditional Security Goals

- ✓ Confidentiality
- ✓ Data Integrity
- ✓ Data origin authentication/
  - entity authentication
- More...
- Authorization
- Privacy
- Non-repudiation
- ...



# SECURITY GOALS

Hi!!! I am Alice



Insecure  
Channel

Hi!!! I am Bob



# SECURITY GOALS

Hi!!! I am Alice



And I am Eve

Hi!!! I am Bob



Insecure  
Channel



This is an attack  
model...



# CONFIDENTIALITY

Hi!!! I am Alice



What are they talking about??

Hi!!! I am Bob



# INTEGRITY

Hi!!! I am Alice



I want to modify their messages

Hi!!! I am Bob



# AUTHENTICATION

Hi!!! I am Alice

Yes, sure! And I am George Clooney

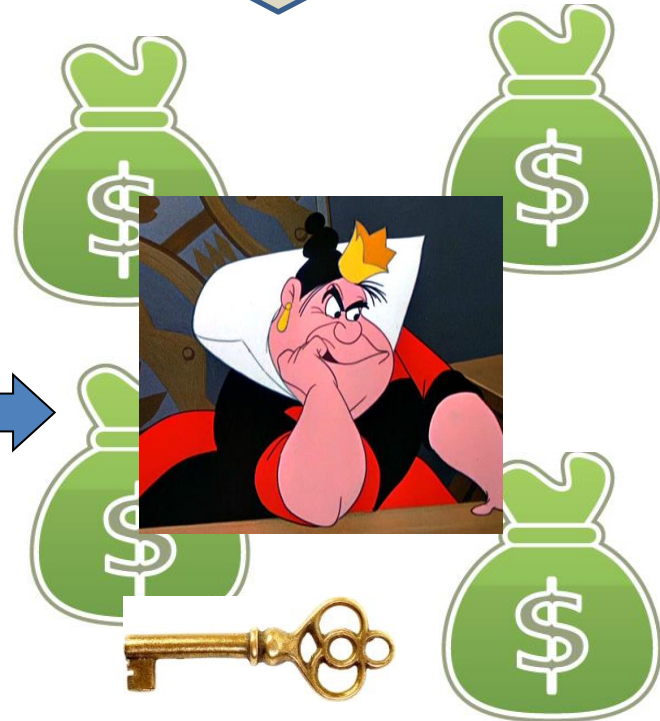


# NON – REPUDIATION

I gave you the money



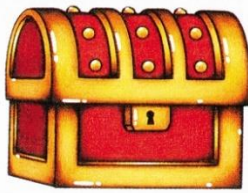
No, you did not!!



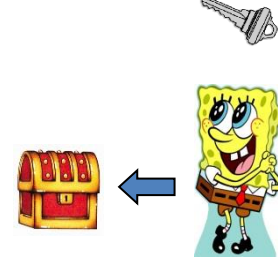
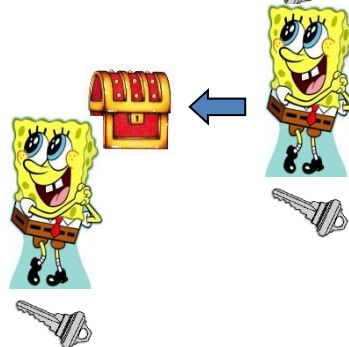
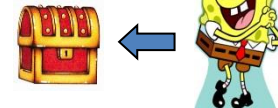
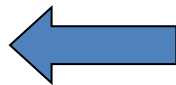
# TYPES OF CRYPTOSYSTEMS

- **Two types of cryptosystems**
  1. Symmetric key
  2. Asymmetric or public key

# SYMMETRIC KEY VS PUBLIC KEY



Secret key



Key Pair



Private Key



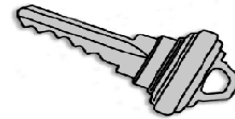
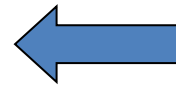
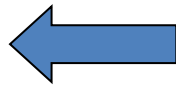
Public Key



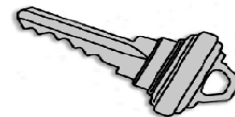
# ASYMMETRIC KEY (PUBLIC KEY)



**Confidentiality**



**Integrity/Authenticity**



# SYMMETRIC KEY – KEY EXCHANGE



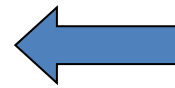
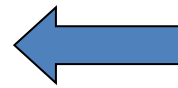
Meeting place



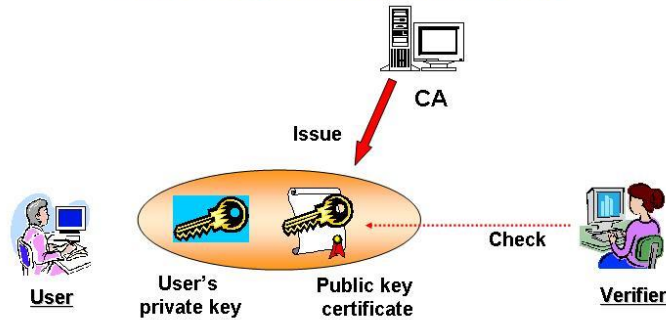
Trusted Third Party (TTP)



# PUBLIC KEY – KEY EXCHANGE



## Public Key Infrastructure (PKI)



Public key infrastructure (PKI)

# Knowledge of encryption algorithms

- Publicly known algorithms
  - ✓ transparency
  - ✓ Interoperability
  - ✓ Usually more secure
- Proprietary algorithms
  - Used only in closed environments

# Auguste Kerckhoffs

- A cryptosystem should not be required to be secret in order to be secure.



**(Jean-Guillaume-Hubert-Victor-François-  
Alexandre-Auguste Kerckhoffs von Nieuwenhof)**

# Type of security

- Unconditional security
  - No assumptions on the adversary
  
- Computational security
  - Assumptions on the resources of the adversary
    - Time
    - Power
    - Memory
    - Data

# Preliminaries

- Modern cryptography is based on a gap between
  - efficient algorithms for encryption for the legitimate users
  - versus the computational infeasibility of decryption for the adversary
- Requires that we have available primitives with certain special computational hardness properties.

# Security definitions

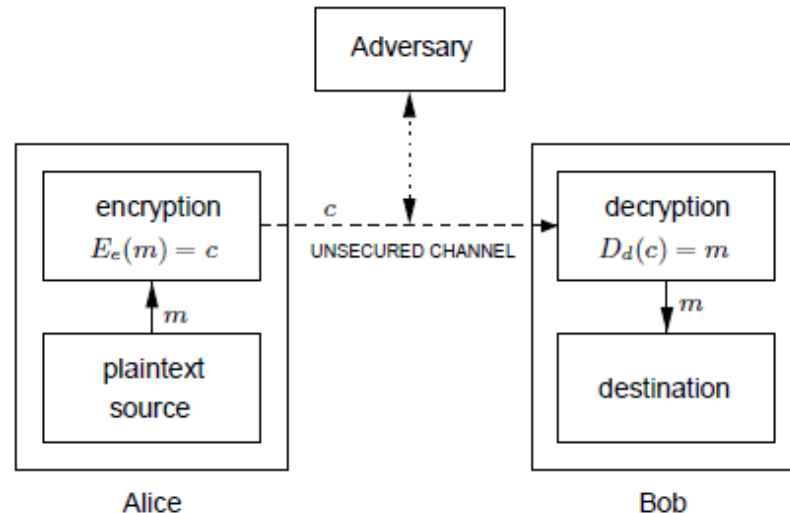
- ▶ Define the attack scenario
- ▶ Define the adversary (computational power, etc)
- ▶ Define the security goal (confidentiality of data)
  
- ▶ There are **MANY DEFINITIONS!!!**

# Adversary model

- Passive
  - Usually an eavesdropper
  - Honest but curious
  
- Active
  - She can modify the messages
  - more powerful adversary
  - can request a polynomial number of ciphertexts to be decrypted for him
  - intercept messages being transmitted from sender to receiver and either stop their delivery all together or alter them in some way

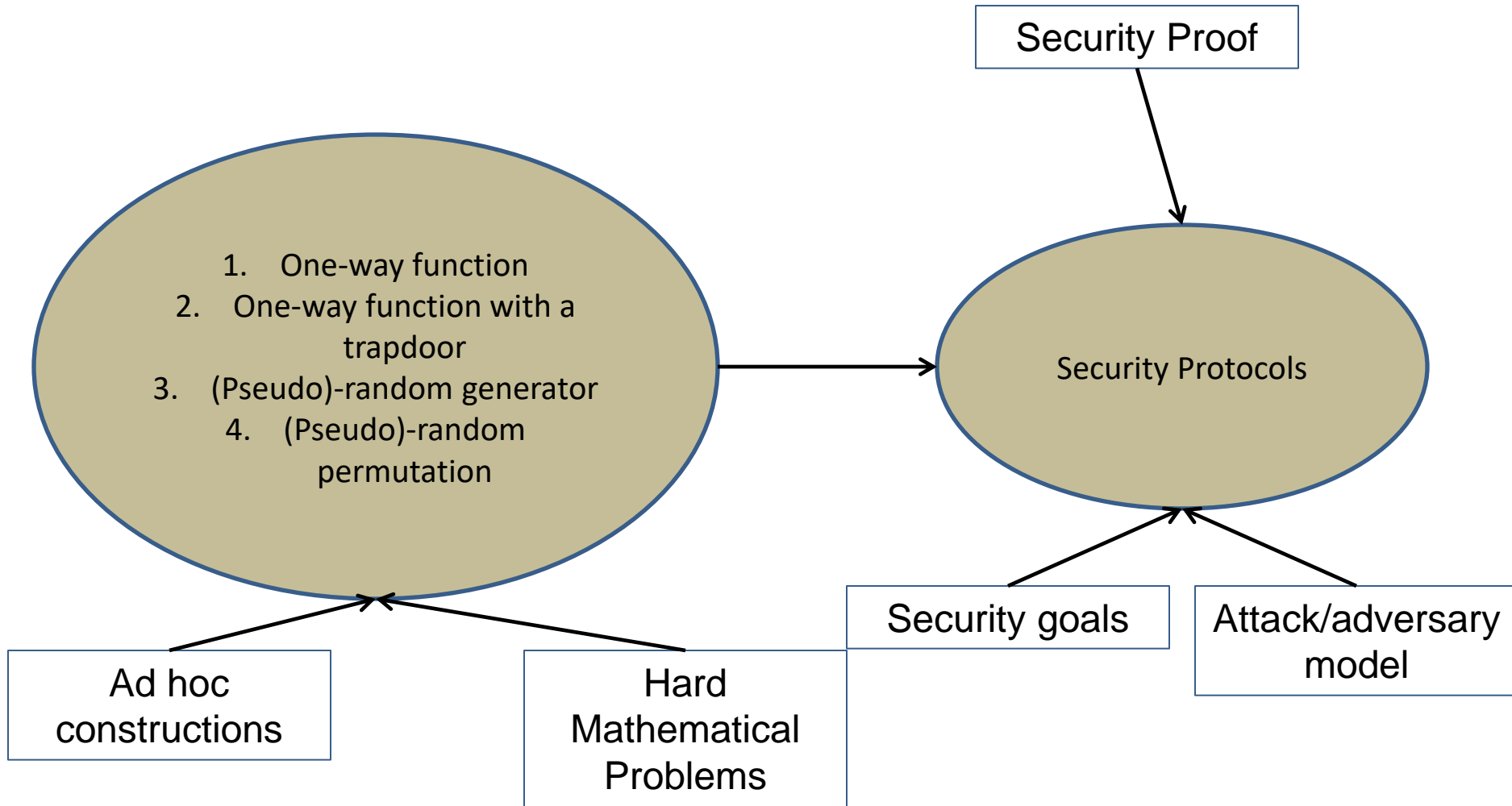
# Theoretical attack scenarios

- 1) Ciphertext-only attack
- 2) Known-plaintext attack
- 3) Chosen-plaintext attack (CPA)
- 4) Adaptive chosen-plaintext attack
- 5) Chosen-ciphertext attack (CCA)
- 6) Adaptive chosen-cip





# BASIC STEPS



# When cryptography is 'broken'?

- When there is an attack that violates one of the security goals
- The attack is more efficient than the security parameter.
- Never assume that an algorithm or protocol can offer more than it was designed for.
- 
- It must be evaluated first!

# Classes of attacks

1. Generic attacks
  - key guessing (exhaustive search)
2. Primitive specific
3. Algorithm specific
4. Side-channel attack
  - Bad implementations

# Exhaustive search

- ✓ Also known as brute force
- ✓ Try to guess the key
- ✓ This attack always exists
  
- There are trade-offs between real-time and precomputation trade-off based on the birthday paradox
  
- You can avoid the attack by increasing the key space (key length)
  
- Modern algorithms have key length at least 128 bits.
  
- Top secret applications need 256 bits security

# Key size

- ✓ How many binary keys of length 256 are there?
- ✓ Key space =  $2^{256}$
  
- ✓ How big is that?
- ✓ Approximately,  $3.31 \times 10^{56}$ .
  
- ✓ This is roughly equal to the number of atoms in the universe!
  
- ✓ The Sunway TaihuLight in China is capable of a peak speed of 93.02 petaflops.
- ✓ That means, it needs 885 quadrillion years to brute force a 128-bit AES key.

# Practical vs theoretical attacks

- Real world attacks
  - Exploit weaknesses of a real system and violate security goals
- Theoretical (or academic) attacks
  - An attack that it is more efficient than the alleged bound, but still far from practical

# Practical vs theoretical attacks

- Example:
- Theoretical:
- there is an attack against AES that allows to crack the algorithm four times faster than was possible previously.
- In practice:
- If you have a trillion machines, that each could test a billion keys per second, it would take more than two billion years to recover an AES-128 key.

# What is the best we can hope for

1. The primitive is solid
2. The algorithm and the protocol are secure
3. The implementation flawless

- Then, it is all about the secret keys.



- Manage the circle of life of a key
- (generate the key, establish, use, store, delete/archive)
- Much more difficult than it sounds!!



# OTHER ATTACKS...



©2001 HowStuffWorks



# **CRYPTOGRAPHIC HISTORY**

# A very old story...

- We can identify the 4 main historical periods:
  1. 4000 BC until WW II
  2. WW II until the 70s
  3. The 70s until today
  4. The Quantum Computing Era

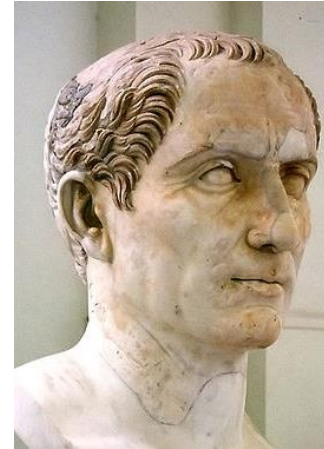
# FIRST PERIOD – HIGHLIGHTS!



# First period – highlights!

- Caesar's Cipher

plaintext digit	A	B	C	D	...	T	U	V	Z
ciphertext digit	D	E	F	G	...	Z	A	B	C



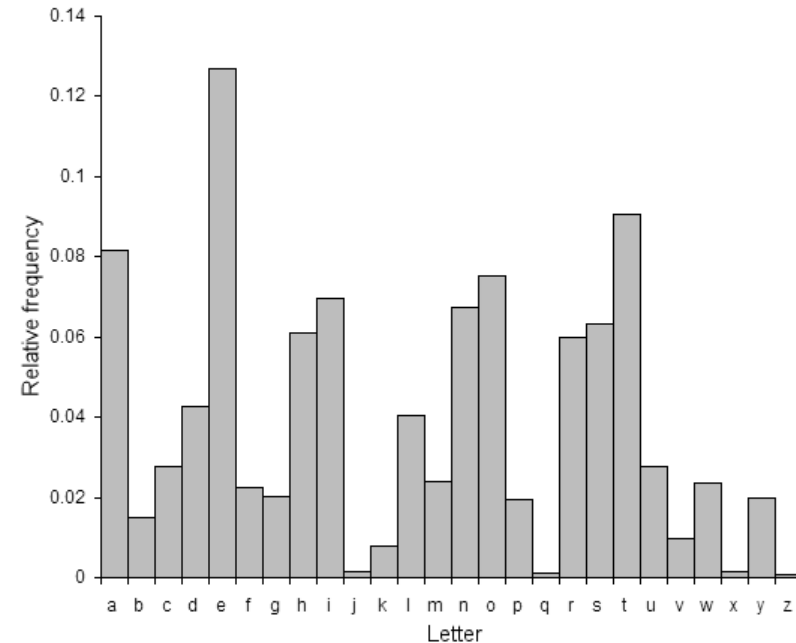
- A substitution cipher
- Symmetric
- Secret key: the number of shifts. Naively always equal to 3. The size of keyspace is 26.
- Plaintext/Ciphertext: the letters of the alphabet from A to Z.
  - Several variations of the cipher.
    - Simple substitution
    - Polyalphabetic substitution

# First period – highlights!

- Cryptosystem – simple substitution
- Secret key: The size of keyspace is  $26!$  (factorial) =  $4 \times 10^{26}$
- $n! = n \times (n-1) \times \dots \times 1$
- *Example*
- plain alphabet : a b c d e f g h i j k l m n o p q r s t u v w x y z
- cipher alphabet: p h q g l u m e a y l n o f d x j k r c v s t z w b
- plaintext: defend the east wall of the castle
- ciphertext: giuifg cei iprc tpnn du cei qprcni

# Substitution Cipher Cryptanalysis

- Frequency analysis
- The ciphertext does not hide the statistics of plaintext
  - <http://substitution.webmasters.sk/simple-substitution-cipher.php>



- Letter average frequency

# Other classical ciphers

- *Vigenère cipher*
- First described by Giovan Battista Bellaso
- in 1553.



- *Playfair cipher*
- It was invented by Charles Wheatstone,
- who first described it in 1854.



- *Vernam cipher*
- Named after Gilbert Sandford Vernam
- who invented it in 1917.





# Second period - WWII

- Enigma

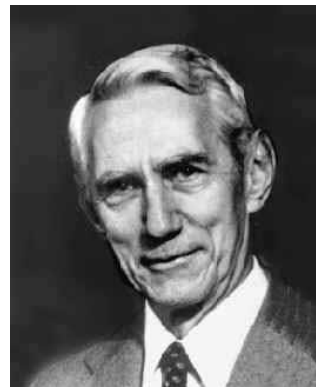


A. Turing

(23/6/1912 –7/6/ 1954)

(1949):«Communication Theory of Secrecy Systems», Bell System Technical Journal, vol.28(4), page 656–715, 1949.

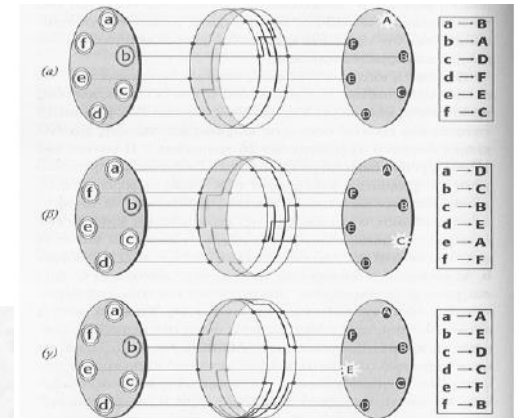
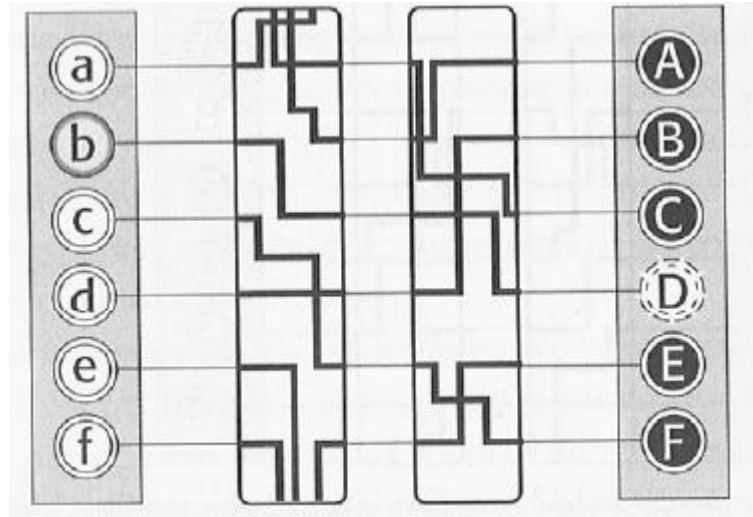
Team (hut) 8, Bletchley Park



C. Shannon

(30/4/1916 –24/2/ 2001)

# Enigma



# Third Period

- The new era



- Well studied algorithms and protocols
- Academia (Bsc courses, Msc programs, research)
- Commercial applications
- Standardization bodies
- Certification
- Several billions market
- Cyberwars and allinces

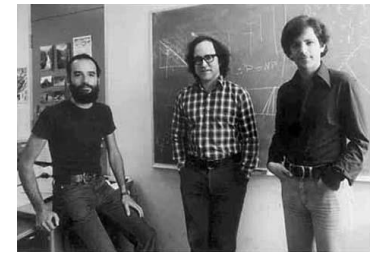


# Third Period

- 1976: «New Directions in Cryptography», in
- IEEE Transactions on information theory by
- Bailey Whitfield Diffie and Martin Hellman
  
- 1977: Data Encryption Standard (DES) becomes
- official Federal Information Processing Standard (FIPS)
- for the United States
  
- 1978: RSA algorithm (Rivest – Shamir – Adleman)
  
- January 14, 2000: U.S. Government announce restrictions on
- export of cryptography are relaxed
  
- 2001: Rijndael algorithm selected as the U.S. Advanced Encryption
- Standard (AES) after a five-year public search process by
- National Institute for Standards and Technology (NIST)



Bailey Whitfield Diffie  
Martin Hellman



# Challenges and open problems

1. Lightweight cryptography for IoT



2. Big data cryptography



3. AI cryptography

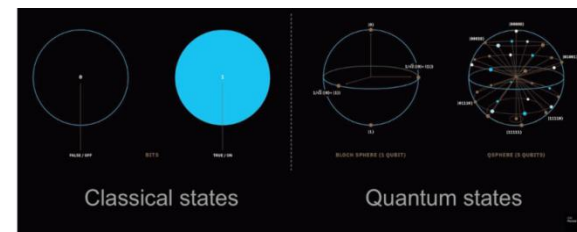


4. Post Quantum Cryptography



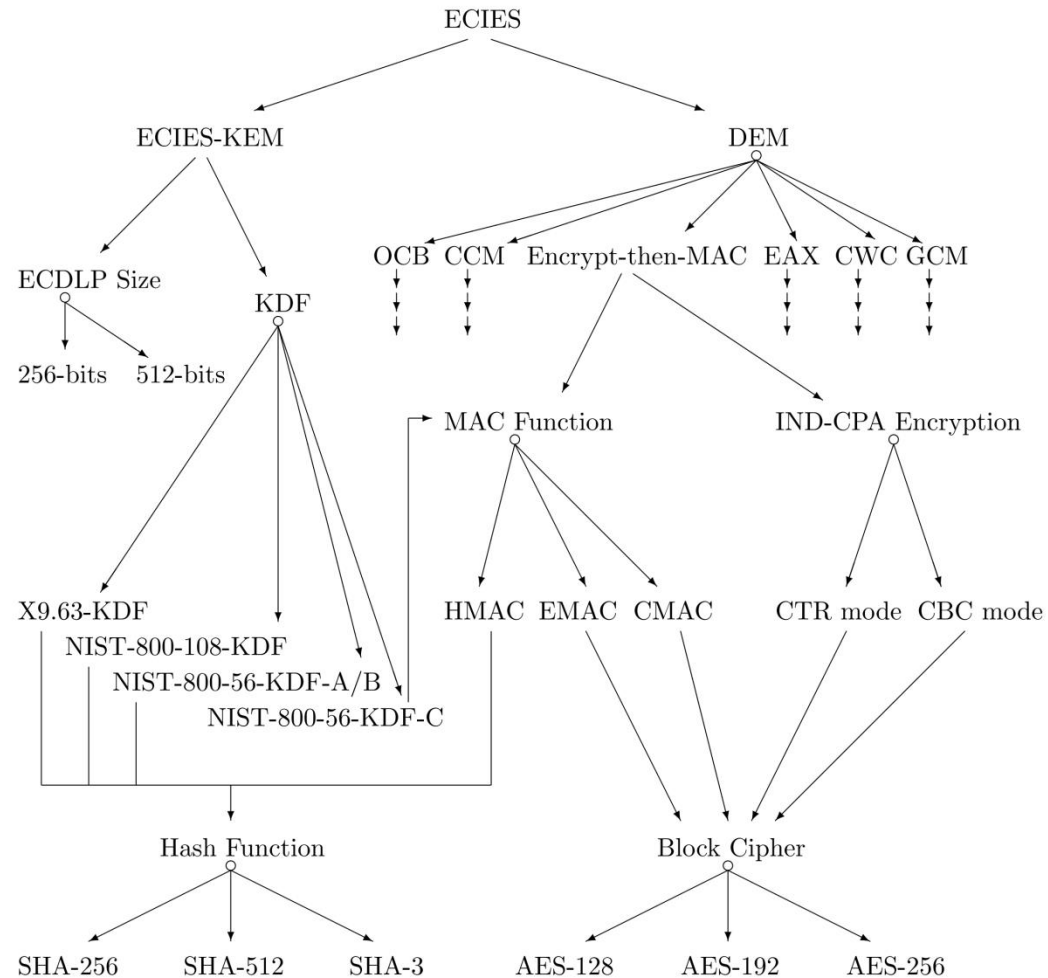
# Fourth period

- 1981 - Richard Feynman proposed
- quantum computers.
  
- Most of the cryptographically interesting hard mathematical problems can be solved efficiently.
  
- PQ standardization competition by NIST
  
- <https://csrc.nist.gov/Projects/Post-Quantum-Cryptography/Post-Quantum-Cryptography-Standardization>



# **CRYPTO AGENDA**

# Overview



\* Algorithms, key size and parameters report. ENISA– 2014

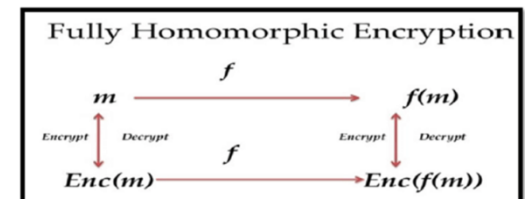
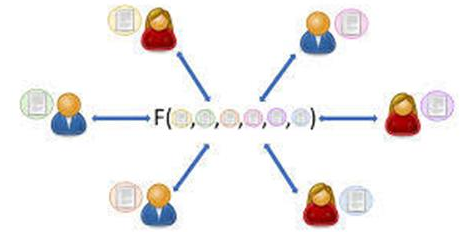


# Classification

Classification	Meaning
Legacy ✗	Attack exists or security considered not sufficient. Mechanism should be replaced in fielded products as a matter of urgency.
Legacy ✓	No known weaknesses at present. Better alternatives exist. Lack of security proof or limited key size.
Future ✓	Mechanism is well studied (often with security proof). Expected to remain secure in 10-50 year lifetime.

# In galaxy (not) so far away

- “Traditional” Cryptography is dealing with
  - P2P security (secure channel)
  - Storage
  - Authentication of data
- We are rapidly moving to the advance Crypto era (confidential computation)
  - Multiparty Computation
  - (Fully) Homomorphic Encryption
  - Zero knowledge proofs (ZK-SNARKs)



# References

- Everyday Cryptography: Fundamental Principles and Applications, Keith M. Martin, oxford press
- The Code Book: The Science of Secrecy from Ancient Egypt to Quantum Cryptography, Simon Singh
- New directions in Cryptography
- <https://ee.stanford.edu/~hellman/publications/24.pdf>
- ECRYPT II Yearly Report on Algorithms and Keysizes (2011-2012)
- ENISA, Algorithms, key size and parameters, report – 2014
- ECRYPT – CSA, Algorithms, Key Size and Protocols Report (2018)

# References

- Lecture Notes on Cryptography, Shafi Goldwasser, 1 Mihir Bellare (check the reading material folder)
- Handbook of Applied Cryptography, Alfred J. Menezes, Paul C. van Oorschot, Scott A. Vanstone (too old, but free) <http://cacr.uwaterloo.ca/hac/>
- Introduction to Modern Cryptography, Jonathan Katz and Yehuda Lindell (2nd Edition!)
- Cryptography Made Simple. Nigel Smart. Springer
- <http://www.cs.umd.edu/~jkatz/imc.html>
- Papers
- Other books

Questions?

