



Cryptography Lecture – Symmetric key Cryptanalysis

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Agenda

- Encryption Security
- Padding attack
- Hash security
- MAC security

Confidentiality

SYMMETRIC ENCRYPTION SCHEMES

Security

- perfect security,
 - an information-theoretic notion introduced by Shannon and showed by him to be met by the one-time pad scheme.
 - regardless of the computing power available to the adversary, the ciphertext provides it no information about the plaintext beyond the a priori information it had prior to seeing the ciphertext
 - it requires a key as long as the total amount of data encrypted
- computational security
 - The security will only hold with respect to adversaries of limited computing power.

Shannon's perfect secrecy definition

Let (E,D) be a cipher over (K,M,C)

(E,D) has perfect secrecy if $\forall m_0, m_1 \in M$ ($|m_0| = |m_1|$) {E(k,m_0)} = {E(k,m_1)} where k (K

One-time pas has perfect secrecy



Perfect Secrecy

Theorem

One time pad has perfect secrecy.

• Proof: easily using Information Theory

Theorem

Perfect secrecy implies that the size of the key K (i.e. the Onetime pad's random sequence) must be greater or equal to plaintext M

Thus, the key must be used only once. Impractical!



Can a stream cipher have perfect secrecy?

Yes, if the PRG is really "secure"

No, there are no ciphers with perfect secrecy

Yes, every cipher has perfect secrecy

No, since the key is shorter than the message



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Two times padding/ re-using the IV (attack 1)

- Let
 - c1 = m1 ⊕ RS
 - c2 = m2 ⊕ RS
- Eve eavesdrops c1,c2

<u>1st attack: Known Plaintext Attack</u> Let m1 be a known plaintext to Eve. Then trivially:

$c1 \oplus c2 \oplus m1 = m1 \oplus RS \oplus m2 \oplus RS \oplus m1 = m2$

• Alice (two times the same keystream)

m1:	0110111	Æ	m2:	1001011	Ĥ
RS:	1011010		RS:	1011010	•
c1:	1 1 0 1 1 0 1		c2:	0010001	

• Eve

m1:	0110111	
c2:	0010001	\frown
c1:	1 1 0 1 1 0 1	\oplus
m2:	1001011	

Stream Ciphers

- One time padding is also a stream cipher requirement, since the same attack applies
- Remember that:
 - The generator PRG produces a pseudorandom sequence PRS
 - PRS=PRG(K,IV)
 - $c = m \bigoplus PRS$

Stream Ciphers (synchronous)



Stream Ciphers

- When the same key/IV pair is used the generator produces the same PRS
- Thus, we have
 - $-c1 = m1 \bigoplus PRS$
 - $-c2 = m2 \oplus PRS$
- The same attach. The IV must never repeat for the same key.

• Alice (two times the same IV)

m1: 0110111	H	m2:	1001011	Ð
PRS: 1011010		PRS:	1011010	
c1: 1 1 0 1 1 0 1		c2:	0010001	

• Eve

m1:	0110111	
c2:	0010001	\frown
c1:	1 1 0 1 1 0 1	\oplus
m2:	1001011	

Two times padding/ re-using the IV (attack 2)

• Let

- $c1 = m1 \oplus RS$ (or PRS)
- $c2 = m2 \oplus RS (or PRS)$
- Eve eavesdrops c1,c2

<u>2nd attack: Known Plaintext Statistics</u>

• Eve computes:

 $\mathsf{c=c1} \oplus \mathsf{c2=m1} \oplus \mathsf{RS} \oplus \mathsf{m2} \oplus \mathsf{RS} = \mathsf{m1} \oplus \mathsf{m2}$

- Eve combines the (most probable) values of m1 and m2 until she produces c
- It is an efficient way to find candidate pairs (m1,m2)

• Alice (two times the same keystream)

				1 0 0 1 0 1 1	
m1:	0110111	Ð	m2:	1001011	Ĥ
k:	1011010		k:	1011010	•
c1:	1 1 0 1 1 0 1		c2:	0010001	

• Eve



Trivial leakage:

When the bits of c are zero then the corresponding bits of m1 and m2 are the same

• Eve

Scenario:

Let any m used by Alice be of the form m=X||D where X is one of {111, 010,011,000}.

Then, m1 = X1|D1 and m2= X2|D2

We have that for the different possible X:

 $111 \oplus 010 = 101$ $111 \oplus 011 = 100$ $010 \oplus 011 = 001$ $111 \oplus 000 = 111$ $011 \oplus 000 = 011$ $010 \oplus 000 = 010$

Since the last 3 bits of c are 100, then the last 3 of m1, m2 are {111,011}/ we don't know which is which.

We can improve the attack we more ciphertexts

Recall Shannon's perfect secrecy

Let (E,D) be a cipher over (K,M,C)

(E,D) has perfect secrecy if $\forall m_0, m_1 \in M$ ($|m_0| = |m_1|$) { E(k,m_0) } = { E(k,m_1) } where k \leftarrow K

(E,D) has (almost) perfect secrecy if $\forall m_0, m_1 \in M (|m_0| = |m_1|)$

 $\{ E(k,m_0) \} \approx_p \{ E(k,m_1) \}$ where $k \leftarrow K$

... but also need adversary to exhibit $m_0, m_1 \in M$ explicitly

Semantic Security/ IND-CPA

For b=0,1 define experiments EXP(0) and EXP(1) as:



for b=0,1: $W_b := [$ event that EXP(b)=1]

 $Adv_{ss}[A,E] := | Pr[W_0] - Pr[W_1] | \in [0,1]$

Semantic Security (one-time key)

Def: \mathbb{E} is **semantically secure** if for all efficient A

 $Adv_{ss}[A, \mathbb{E}]$ is negligible.

- Indistinguishability under chosen-plaintext attack (IND-CPA)

 \Rightarrow for all explicit m_0 , $m_1 \in M$:

 $\{ E(k,m_0) \} \approx_p \{ E(k,m_1) \}$

Suppose efficient A can always deduce LSB of PT from CT.

 \Rightarrow E = (E,D) is not semantically secure.



Then $Adv_{ss}[B, E] = |Pr[EXP(0)=1] - Pr[EXP(1)=1]| = |0-1| = 1$

- When algorithm A works with probability p (not certain) then the attack is the same, only the advantage changes.
- Example, p = 0.8

Then $Adv_{ss}[B, E] = |0,8-0,2| = |0,6| = 0,6$

 Έστω ότι ο (E,D) είναι ένας semantically secure cipher όπου ο χώρος του μηνύματος και του ciphertext είναι {0,1}ⁿ. Εϊναι το ακόλουθο σχήμα κρυπτογράφησης είναι semantically secure?

 $E'(k,m)=E(k,m)||||(LSB(m) \bigoplus MSB(m))$

Proof (sketch):

- 1. Use the definition to evaluate the scheme
- 2. We are looking for two messages such that LSB(m)⊕ MSB(m) gives different output
- 3. Two such messages, for any m, are
 - -m0 = (0||m||0)
 - m1 = (1||m||0)

(there are also other choices of course.)

• The advantage is 1.

Suppose efficient A can always deduce LSB \oplus MSB of PT from CT.

 \Rightarrow E = (E,D) is not semantically secure.



Then $Adv_{ss}[B, E] = |Pr[EXP(0)=1] - Pr[EXP(1)=1]| = |0-1| = 1$

Block Cipher ECB Mode

Encryption



Electronic Codebook (ECB) mode encryption

Example 3 (ECB mode)

Suppose that ECB mode of a block cipher B is used.

E = (E,D) is not semantically secure. \Rightarrow



Then $Adv_{ss}[B, E] = |Pr[EXP(0)=1] - Pr[EXP(1)=1]| = |0-1| = 1$

PADDING

Padding

- Padding it is needed when the input doesn't have the necessary length.
 - For instance when a plaintext is processed in blocks (CBC mode, ECB mode etc
 - When message is processed in blocks (hash functions)
- There are padding oracle attacks
 - An application exhibits padding errors while decrypting a ciphertext
 - The attacker can choose the ciphertext (chosen ciphertext attack)
 - (for instance keywrapping)

Padding in CBC mode



Padding

- There are several padding schemes
 - Zero padding (ex. CBC-CS1/2/3, NIST Special Publication 800-38A)
 - One and zeros padding
 - PKCS5/PKCS7

PKCS5 Padding

- Originally designed for block ciphers operating on 64-bit blocks (e.g., DES).
- Up to 8-bytes (64-bit) block sizes.
- The plaintext is padded by adding bytes, each of which is the number of padding bytes added.
 - Example, if 3 bytes of padding are added, the padding will be 0x03 0x03 0x03.
 - if 5 bytes of padding are added, the padding will be 0x05 0x05 0x05 0x05 0x05.

PKCS7 Padding(similar to PKCS5)

- Supports block sizes of up to 255 bytes (maximum number stored in a byte).
- if a message is a multiple of blockSize, PKCS7 still "pads out" with a block of 16 0x10s

PKCS7

Value of clear text length (mod 16)	Number of padding bytes added	Value of each padding byte
0	16	0x10
1	15	0x0F
2	14	0x0E
3	13	0x0D
4	12	0x0C
5	11	0x0B
6	10	0x0A
7	9	0x09
8	8	0x08
9	7	0x07
10	6	0x06
11	5	0x05
12	4	0x04
13	3	0x03
14	2	0x02
15	1	0x01

Single block attack

The encrypted message consists of an IV and a single ciphertext block.

- We can set the IV to whatever we want. Initially IV is all zeros
- The padding oracle will compute tells us only whether or not the resulting plaintext block ends with valid padding.
- By making modifications to the IV, we can predictably modify the plaintext block, since flipping a bit in the IV will flip the corresponding bit in the plaintext.
- Setting the IV's final byte to any value will xor that value into the plaintext's final byte.
- If we iterate through every possible value for the final IV byte, eventually one of them will set the plaintext's final byte to 0x01
 - The padding oracle will tell us when this happens, because 0x01 is valid padding!
 - A trailing 0x01 byte meets the padding standard, so the oracle accepts it just like it would accept 0x02 0x02 or 0x03 0x03 0x03.
Padding Attack (1)

• Single block messages



Single block attack

- The search for a valid IV byte ends when we reach 0x2e, because $0x2e \oplus 0x2f = 0x01$.
- We can start to construct what I'll call a zeroing IV, i.e. the IV which will set some (eventually all) of the plaintext's bytes to zero.
 - zero gives us options. If we want to set a plaintext byte to any value other than zero, we can just xor that value into the zeroing IV.
 In other words, the zeroing IV gives us a way of manipulating the plaintext however we like.
- As soon as we set the plaintext's final byte to 0x01, we can take the corresponding IV byte and xor that against 0x01. This modified IV byte will set the plaintext's final byte to 0x00 and so it will work as the final byte of our zeroing IV.
- Once we have that, we can derive a new IV which is guaranteed to set the plaintext's final byte to 0x02, and we can start trying to set the plaintext's penultimate byte to 0x02 as well.
- Once we've found valid one-byte padding, we can use a similar process to search for valid two-byte padding.
- This search will terminate when the plaintext's final two bytes equal 0x02 0x02. This permits us to move on to attacking the third-from-last byte, then the fourth-from-last, and so on.
- Note: If the plaintext's penultimate byte is already set to 0x02, then the message's padding would be valid if the final byte is set to either 0x01 or 0x02. If our ultimate byte search hits 0x02 before 0x01, but we assume that we found 0x01 and not 0x02, and the attack fails. We get an affirmative result from the oracle, by changing the IV's penultimate byte and query the oracle again. If both queries succeed, this tells us that the penultimate byte is not part of the message's (valid) padding, proving that the padding has length one and thus must have value 0x01 as well. On the other hand, if this second query fails, we've run into a false positive and should keep searching.

Padding Attack (2)

• Single block messages



Padding Attack

- The attack can be generalized to multi-block plaintexts [1]
- A real world attack against TLS 1.2, IPsec
 - It takes advantage of MAC-then-encrypt
- This attack was first reported against TLS by Serge Vaudenay in 2002 [2].

[1] <u>https://www.nccgroup.com/us/research-blog/cryptopals-exploiting-cbc-padding-oracles/</u>

[2] https://www.iacr.org/archive/eurocrypt2002/23320530/cbc02_e02d.pdf

HASH FUNCTIONS

Cryptographic properties



Cryptanalysis

We can do one of the following:

1)Show that there is an attack more efficient than the generic attacks, i.e.

- Guess a preimage (complexity 2ⁿ)
- Guess a 2nd preimage (complexity 2ⁿ)
- ✓ Guess a collision pair (complexity 2^{n/2})

2)Build on a secure primitive and prove that the construction is secure by showing that if there is an efficient attack against the construction then you can adapt this attack and mount a new one against the secure primitive.

Exercise 1

Let $H:\{0,1\}^* \rightarrow T$ be a collision resistant hash function. Is the following hash function collision resistant?

 $H'(m)=H(m)\oplus H(m\oplus 1^{|m|})$

where |m| is length of m and 1^x is a string of x 1's.

For instance, let m=10101. Then, |m|=5 and 1^{|m|}=1⁵=11111



Exercise 1

Proof

Clearly, it is easy to show that any two message m, m' such that m' = $m \oplus 1^{|m|}$, they have that same hash value:

 $H'(m')=H(m')\oplus H(m'\oplus 1^{|m'|})=H(m\oplus 1^{|m|})\oplus H(m\oplus 1^{|m|}\oplus 1^{|m|})=$

 $= H(m \oplus 1^{|m|}) \oplus H(m) = H'(m)$

Thus, it is not collision resistant.

(Try as an example the pair (m = 110001, m' = 001110)



Exercise 2

 Let H: {0,1}*→{0,1}ⁿ be a collision resistant hash function. Is the following hash function collision resistant? H'(m)=H(H(m))



Proof (sketch)

Let

•

H'(m)=H(H(m))

and let's assume that H'(m) is not collision resistant.

Thus, there is a **polynomial algorithm A** that can compute a pair of **different** messages **m1** and **m2**, more efficiently than $O(2^{n/2})$, such that:

H'(m1)=H'(m2)

Thus, it holds

H(H(m1))=H(H(m2)).

Proof (sketch)

Thus, it holds

H(H(m1))=H(H(m2)).

We distinguish two cases:

1. H(m1)=H(m2). Then, the algorithm A can compute collisions for H(m), more efficiently than $O(2^{n/2})$. **This is a contradiction.**

 H(m1)≠H(m2). Then, the messages y1=H(m1) and y2=H(m2) H(H(m1))=H(H(m2)) <=> H(y1)=H(y2)

are collisions for H(m). That is that, the algorithm A can compute collisions for H(m), more efficiently than $O(2^{n/2})$. This is a contradiction.

MAC SECURITY

Strong Unforgeability under Chosen Message Attack (SUF-CMA)

• For a MAC I=(S,V) and adv. A define a MAC game as:



Def: I=(S,V) is a <u>secure MAC</u> if for all "efficient" A: Adv_{MAC}[A,I] = Pr[Chal. outputs 1] is "negligible."

(RAW) CBC-MAC security



(RAW) CBC-MAC security

• Let m = D0

(size single block)

• Let m' = $D0||D0 \oplus tag$

(size two blocks)



Strong Unforgeability under Chosen Message Attack (SUF-CMA)



b=1

 $Adv_{MAC}[A,I] = Pr[Chal. outputs 1]=1$

Example

Lets assume that the ECBC_{IV} is a modified version of EMAC which uses a randomly selected **IV** for each message **m** and produces the output as it appears in the next slide. The IV will then be part of the tag, i.e.

tag=(IV, ECBC_{IV}(k,k',m))

where (k,k') are the two keys. Is the new MAC SUF-CMA secure?

Modified EMAC (ECBCIV)



Modified EMAC (ECBCIV)



 Let m₁ = D₀. Then, tag=(IV, ECBC_{IV}(k,m₁))
 and IV ⊕D₀ is the input of the cipher F

Modified EMAC (ECBCIV)



ECBC-MAC and HMAC analysis

<u>Theorem</u>: Let q be the number of different messages for which a tag was produced (using the same key) and let L be the total length in bits. If Adv[B,F] be the advantage of an efficient attacker B against a block cipher F and Adv[B,H] be the advantage of an efficient attacker B against a hash function H. Then:

 $Adv_{PRF}[A, F_{ECBC}] \le Adv_{PRP}[B, F] + 2 q^2 / |X|$

 $Adv_{PRF}[A, F_{HMAC}] \leq q \cdot L \cdot Adv_{PRF}[B, F] + q^2 / 2 |K|$

Where |X| is the total number of different input blocks for the block cipher and |K| the total number of keys

ECBC-MAC and HMAC analysis

1. When the block cipher is secure we Adv[B,F]=0 and

 $Adv_{PRF}[A, F_{ECBC}] \leq 2 q^2 / |X|$

Thus, CBC-based MAC is secure as long as $q \ll |X|^{1/2}$

2. When the block cipher is secure we Adv[B,H]=0 and

 $Adv_{PRF}[A, F_{HMAC}] \leq q^2 / 2 |K|$

Thus, HMAC is secure as long as $q \ll |K|^{1/2}$

An example

Adv_{PRF}[A, F_{ECBC}] \leq Adv_{PRP}[B, F] + 2 q² / |X| q = # messages MAC-ed with k

Suppose we want $Adv_{PRF}[A, F_{ECBC}] \le 1/2^{32} \iff q^2 / |X| < 1/2^{32}$

• AES: $|X| = 2^{128} \implies q < 2^{48}$

So, after 2⁴⁸ messages we must change key

• 3DES:
$$|X| = 2^{64} \implies q < 2^{16}$$

So, after 2¹⁶ messages we must change key

WEP - SECURITY

Wired Equivalent Privacy (WEP)

- WEP Part of original 802.11 specification published in 1999.
- Confidentiality
 - Uses RC4 Stream cipher
 - Has static 40-bit base key (common for all the clients)
 - A 64-bit per-packet key
 - A 24-bit Initialization Vector (IV)
- Integrity
 - Uses Integrity Check Value (ICV) to verify integrity
 - No key!!

Characteristics - notes

- Stateless protocol
 - Mobile stations and access points are not required to keep past state
- Encrypted CRC-32 used as integrity check
 - Fine for random errors, but not deliberate ones
 - Linear
 - CRC(X+Y) = CRC(X)+CRC(Y)
- RC4 keystream should not be reused
 - One-time pad

Shared-Key Authentication

Prior to communicating data, access point may require client to authenticate



Shared-Key Authentication

Prior to communicating data, access point may require client to authenticate



Attack on Access Control



- It is possible to get authenticated without knowing the secret key! (shown in blue)
- We only need a plaintext, ciphertext pair of a legitimate authentication. (shown in black)

How WEP "Privacy" Works



no integrity!

WEP



WEP



- Share a single cryptographic key among all devices
- Encrypt all packets sent over the air, using the shared key
- Use a checksum to prevent injection of spoofed packets

WEP - A Little More Detail



• WEP uses the RC4 stream cipher to encrypt a TCP/IP packet (P) by xor-ing it with keystream (RC4(K, IV))

Attack #1: Keystream Reuse

- WEP didn't use RC4 carefully
- The problem: IV's frequently repeat
 - The IV is often a counter that starts at zero
 - Hence, rebooting causes IV reuse
 - Also, there are only 16 million possible IV's, so after intercepting enough packets, there are sure to be repeats
- > Attackers can eavesdrop on 802.11 traffic
 - An eavesdropper can decrypt intercepted ciphertexts even without knowing the key

Attack #2: Spoofed Packets

- Attackers can inject forged 802.11 traffic
 - Learn RC4(K, IV) using previous attack
 - Since the checksum is unkeyed, you can then create valid ciphertexts that will be accepted by the receiver
A Property of RC4

- Keystream leaks, under known-plaintext attack
 - Suppose we intercept a ciphertext C, and suppose we can guess the corresponding plaintext P
 - Let PRS = RC4(K, IV) be the RC4 keystream
 - Since $C = P \oplus PRS$, we can derive the RC4 keystream PRS by $P \oplus C = P \oplus (P \oplus PRS) = PRS$
- This is not a problem ... unless keystream is reused!

A Risk of Keystream Reuse



- If IV's repeat, confidentiality is at risk
 - If we send two ciphertexts (C, C') using the same IV, then the xor of plaintexts leaks ($P \oplus P' = C \oplus C'$), which might reveal both plaintexts

Lesson: If RC4 isn't used carefully, it becomes insecure

A note on IVs

- What if random IVs were used?
- IV space 2²⁴ possibilities
- Collision after 4000 packets
- Rough estimate: a busy AP sends 1000 packets/sec
- Collision every 4s!
- Even with counting IV (best case), rollover every few hours

So..

 If we have 2²⁴ known plaintexts, can decrypt every packet!!!!

Attack #2: Spoofed Packets



- Attackers can inject forged 802.11 traffic
 - Learn Z = RC4(K, IV) using previous attack
 - Since the CRC checksum is unkeyed, you can then create valid ciphertexts that will be accepted by the receiver

> Attackers can bypass 802.11b access control

- All computers attached to wireless net are exposed

Attack #3: Packet Modification



• CRC is linear \Rightarrow CRC(P $\oplus \Delta$) = CRC(P) \oplus CRC(Δ)

 \Rightarrow the modified packet (P $\oplus \Delta$) has a valid checksum

> Attacker can tamper with packet (P) without breaking RC4

Attack #4: Replay Attacks



Attacker can replay plaintext (P) without breaking RC4
Stateless!!

Attacks

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